

Fira Math

Sans-serif font with Unicode math support

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2019/06/03 v0.3.2

Basic examples (I)

- Covariant derivative:

$$\nabla \mathbf{X} = X^\alpha{}_{;\beta} \frac{\partial}{\partial X^\alpha} \otimes dx^\beta = \left(X^\alpha{}_{;\beta} + \Gamma^\alpha{}_{\beta\gamma} X^\gamma \right) \frac{\partial}{\partial X^\alpha} \otimes dx^\beta$$

- Einstein's field equations:

$$G_{\mu\nu} \equiv R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

- Schwarzschild metric:

$$c^2 d\tau^2 = \left(1 - \frac{r_s}{r}\right) c^2 dt^2 - \left(1 - \frac{r_s}{r}\right)^{-1} dr^2 - r^2 \underbrace{(d\theta^2 + \sin^2 \theta d\varphi^2)}_{d\Omega^2}$$

- Einstein-Hilbert action:

$$S = \frac{1}{2\kappa} \int R \sqrt{-g} d^4x$$

Basic examples (II)

- Case $n = 1$

$$\int_0^{\frac{\pi}{2}} \frac{\sqrt{\frac{1}{2} \sqrt{\frac{\ln^2 \cos \theta}{\theta^2 + \ln^2 \cos \theta}} + \frac{1}{2}}}{\sqrt[4]{\theta^2 + \ln^2 \cos \theta}} d\theta = \frac{\pi}{2\sqrt{\ln 2}}$$

- Generalization:

$$\begin{cases} R_n^- = \frac{2}{\pi} \int_0^{\pi/2} (\theta^2 + \ln^2 \cos \theta)^{-2^{-n-1}} \sqrt{\frac{1}{2} + \frac{1}{2} \sqrt{\frac{1}{2} + \dots + \frac{1}{2} \sqrt{\frac{\ln^2 \cos \theta}{\theta^2 + \ln^2 \cos \theta}}}} d\theta = (\ln 2)^{-2^{-n}} \\ R_n^+ = \frac{2}{\pi} \int_0^{\pi/2} (\theta^2 + \ln^2 \cos \theta)^{2^{-n-1}} \sqrt{\frac{1}{2} + \frac{1}{2} \sqrt{\frac{1}{2} + \dots + \frac{1}{2} \sqrt{\frac{\ln^2 \cos \theta}{\theta^2 + \ln^2 \cos \theta}}}} d\theta = (\ln 2)^{2^{-n}} \end{cases}$$

Using with CJK fonts

- 【留数定理】 全純函数 f 在若尔当曲线 γ 上的积分为：

$$\oint_{\gamma} f(z) dz = 2\pi i \sum_{k=1}^n \operatorname{Res}_{z=a_k} f(z).$$

- 【留数定理】 全純函数 f 在若爾當曲線 γ 上的積分為：

$$\oint_{\gamma} f(z) dz = 2\pi i \sum_{k=1}^n \operatorname{Res}_{z=a_k} f(z).$$

- 【留数定理】 ジョルダン曲線 γ に沿う正則関数 f の積分は、

$$\oint_{\gamma} f(z) dz = 2\pi i \sum_{k=1}^n \operatorname{Res}_{z=a_k} f(z).$$