Package 'cpfa'

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Type Package

Title Classification with Parallel Factor Analysis

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Depends multiway

Imports glmnet, e1071, randomForest, nnet, rda, xgboost, foreach, doParallel

Description Classification using Richard A. Harshman's Parallel Factor Analysis-1 (Parafac) model or Parallel Factor Analysis-2 (Parafac2) model fit to a three-way or four-way data array. See Harshman and Lundy (1994): <doi:10.1016/0167-9473(94)90132-5>. Uses component weights from one mode of a Parafac or Parafac2 model as features to tune parameters for one or more classification methods via a k-fold cross-validation procedure. Allows for constraints on different tensor modes. Supports penalized logistic regression, support vector machine, random forest, feed-forward neural network, regularized discriminant analysis, and gradient boosting machine. Supports binary and multiclass classification. Predicts class labels or class probabilities and calculates multiple classification performance measures. Implements parallel computing via the 'parallel' and 'doParallel' packages.

License GPL (>= 2)

NeedsCompilation no

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Contents

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cpfa   *Classification with Parallel Factor Analysis*

Description

Fits Richard A. Harshman's Parallel Factor Analysis-1 (Parafac) model or Parallel Factor Analysis-2 (Parafac2) model to a three-way or four-way data array. Allows for different constraint options on multiple tensor modes. Uses Parafac component weights from a single mode of this model as predictors to tune parameters for one or more classification methods via a k-fold cross-validation procedure. Predicts class labels and calculates multiple performance measures for binary or multi-class classification across multiple replications with different train-test splits. Provides descriptive statistics to pool output across replications.

Usage

```
cpfa(x, y, model = c("parafac", "parafac2"), nfac = 1, nrep = 5, ratio = 0.8,
     nfolds = 10, method = c("PLR", "SVM", "RF", "NN", "RDA", "GBM"),
     family = c("binomial", "multinomial"), parameters = list(),
     type.out = c("measures", "descriptives"), foldid = NULL,
     prior = NULL, cmode = NULL, seeds = NULL, plot.out = FALSE,
     plot.measures = NULL, parallel = FALSE, cl = NULL, verbose = TRUE, ...)
```

Arguments

x	A three-way or four-way data array. For Parafac2, can be a list where each element is a matrix or three-way array. Array or list must contain only real numbers. See note below.
y	A vector containing at least two unique class labels. Should be a factor that contains two or more levels. For binary case, ensure the order of factor levels (left to right) is such that negative class is first and positive class is second.
model	Character designating the Parafac model to use, either model = "parafac" to fit the Parafac model or model = "parafac2" to fit the Parafac2 model.
nfac	Number of components for each Parafac or Parafac2 model to fit. Default is nfac = 1.
nrep	Number of replications to repeat the procedure. Default is nrep = 5.
ratio	Split ratio for dividing data into train and test sets. Default is ratio = 0.8.
nfolds	Numeric value specifying number of folds for k-fold cross-validation. Must be 2 or greater. Default is nfolds = 10.

method   Character vector indicating classification methods to use. Possible methods include penalized logistic regression (PLR); support vector machine (SVM); random forest (RF); feed-forward neural network (NN); regularized discriminant analysis (RDA); and gradient boosting machine (GBM). If none are selected, default is to use all methods with method = c("PLR", "SVM", "RF", "NN", "RDA", "GBM").

family   Character value specifying binary classification (family = "binomial") or multiclass classification (family = "multinomial"). If not provided, number of levels of input y is used, where two levels is binary, and where three or more levels is multiclass.

parameters   List containing arguments related to classification methods. When specified, must contain one or more of the following:

alpha Values for penalized logistic regression alpha parameter; default is alpha = seq(0, 1, length = 6). Must be numeric and contain only real numbers between 0 and 1, inclusive.

lambda Optional user-supplied lambda sequence for cv.glmnet for penalized logistic regression. Default is NULL.

cost Values for support vector machine cost parameter; default is cost = c(1, 2, 4, 8, 16, 32, 64). Must be numeric and contain only real numbers greater than or equal to 0.

gamma Values for support vector machine gamma parameter; default is gamma = c(0, 0.01, 0.1, 1, 10, 100, 1000). Must be numeric and greater than or equal to 0.

ntree Values for random forest number of trees parameter; default is ntree = c(100, 200, 400, 600, 800, 1600, 3200). Must be numeric and contain only integers greater than or equal to 1.

nodesize Values for random forest node size parameter; default is nodesize = c(1, 2, 4, 8, 16, 32, 64). Must be numeric and contain only integers greater than or equal to 1.

size Values for neural network size parameter; default is size = c(1, 2, 4, 8, 16, 32, 64). Must be numeric and contain only integers greater than or equal to 0.

decay Values for neural network decay parameter; default is decay = c(0.001, 0.01, 0.1, 1, 2, 4, 8, 16). Must be numeric and contain only real numbers.

rda.alpha Values for regularized discriminant analysis alpha parameter; default is rda.alpha = seq(0, 0.999, length = 6). Must be numeric and contain only real numbers between 0 (inclusive) and 1 (exclusive).

delta Values for regularized discriminant analysis delta parameter; default is delta = c(0, 0.1, 1, 2, 3, 4). Must be numeric and contain only real numbers greater than or equal to 0.

eta Values for gradient boosting machine eta parameter; default is eta = c(0.1, 0.3, 0.5, 0.7, 0.9). Must be numeric and contain only real numbers greater than 0 and less than 1.

max.depth Values for gradient boosting machine max.depth parameter; default is max.depth = c(1, 2, 3, 4). Must be numeric and contain only integers greater than or equal to 1.

	subsample Values for gradient boosting machine subsample parameter; default is subsample = c(0.6, 0.7, 0.8, 0.9). Must be numeric and contain only real numbers greater than 0 and less than or equal to 1.
	nrounds Values for gradient boosting machine nrounds parameter; default is nrounds = c(100, 200, 300, 500). Must be numeric and contain only integers greater than or equal to 1.
type.out	Type of output desired: type.out = "measures" gives array containing classification performance measures for all replications while type.out = "descriptives" gives list of descriptive statistics calculated across all replications for each performance measure. Both options also provide the estimated training weights and classification weights. Defaults to type.out = "descriptives".
foldid	Integer vector containing fold IDs for k-fold cross-validation. If not provided, fold IDs are generated randomly for number of folds nfolds.
prior	Prior probabilities of class membership. If unspecified, the class proportions for input y are used. If specified, the probabilities should be in the order of the factor levels of input y.
cmode	Integer value of 1, 2, or 3 (or 4 if x is a four-way array) specifying the mode whose component weights will be predictors for classification. Defaults to the last mode of the input array (i.e., defaults to 3 for three-way array, and to 4 for four-way array). If model = "parafac2", last mode will be used.
seeds	Random seeds to be associated with each replication. Default is seeds = 1:nrep.
plot.out	Logical indicating whether to output one or more box plots of classification performance measures that are plotted across classification methods and number of components.
plot.measures	Character vector containing values that specify for plotting one or more of 11 possible classification performance measures. Only relevant when plot.out = TRUE. Should contain one or more of the following labels: c("err", "acc", "tpr", "fpr", "tnr", "fnr", "ppv", "npv", "fdr", "fom", "fs"). A box plot will be created for each measure that is specified, summarizing output across replications. Note that additional information about each label is available in the Details section of the help file for function cpm. Note also that there are a few cases where the x-axis tick labels for a plot might not appear. A future update is planned to fix this issue.
parallel	Logical indicating if parallel computing should be implemented. If TRUE, the package **parallel** is used for parallel computing. For all classification methods except penalized logistic regression, the **doParallel** package is used as a wrapper. Defaults to FALSE, which implements sequential computing.
cl	Cluster for parallel computing, which is used when parallel = TRUE. Note that if parallel = TRUE and cl = NULL, then the cluster is defined as makeCluster(detectCores()).
verbose	If TRUE, progress is printed.
...	Additional arguments to be passed to function parafac for fitting a Parafac model or function parafac2 for fitting a Parafac2 model. Example: can impose different constraints on different modes of the input array using the argument const. See help file for function parafac or for function parafac2 for additional details.

Details

Data are split into a training set and a testing set. After fitting a Parafac or Parafac2 model with the training set using package **multiway** (see parafac or parafac2 in **multiway** for details), the estimated classification mode weight matrix is passed to one or more classification methods. The methods include: penalized logistic regression (PLR); support vector machine (SVM); random forest (RF); feed-forward neural network (NN); regularized discriminant analysis (RDA); and gradient boosting machine (GBM).

Package **glmnet** fits models for PLR. PLR tunes penalty parameter lambda while the elastic net parameter alpha is set by the user (see the help file for function cv.glmnet in package **glmnet**). For SVM, package **e1071** is used with a radial basis kernel. Penalty parameter cost and radial basis parameter gamma are used (see svm in package **e1071**). For RF, package **randomForest** is used and implements Breiman's random forest algorithm. The number of predictors sampled at each node split is set at the default of sqrt(R), where R is the number of Parafac or Parafac2 components. Two tuning parameters allowed are ntree, the number of trees to be grown, and nodesize, the minimum size of terminal nodes (see randomForest in package **randomForest**). For NN, package **nnet** fits a single-hidden-layer, feed-forward neural network model. Penalty parameters size (i.e., number of hidden layer units) and decay (i.e., weight decay) are used (see **nnet**). For RDA, package **rda** fits a shrunken centroids regularized discriminant analysis model. Tuning parameters include rda.alpha, the shrinkage penalty for the within-class covariance matrix, and delta, the shrinkage penalty of class centroids towards the overall dataset centroid. For GBM, package **xgboost** fits a gradient boosting machine model. Four tuning parameters are allowed: (1) eta, the learning rate; (2) max.depth, the maximum tree depth; (3) subsample, the fraction of samples per tree; and (4) nrounds, the number of boosting trees to build.

For all six methods, k-fold cross-validation is implemented to tune classification parameters where the number of folds is set by argument nfolds. Separately, the trained Parafac or Parafac2 model is used to predict the classification mode's component weights using the testing set data. The predicted component weights and the optimized classification method are then used to predict class labels. Finally, classification performance measures are calculated. The process is repeated over a number of replications with different random splits of the input array and of the class labels at each replication.

Value

Returns an object of class wrapcpfa either with a three-way array with classification performance measures for each model and for each replication, or with a list containing matrices with descriptive statistics for performance measures calculated across all replications. Specify type.out = "measures" to output the array of performance measures. Specify type.out = "descriptives" to output descriptive statistics across replications. In addition, for both options, the following are also provided:

predweights   List of predicted classification weights for each Parafac or Parafac2 model and for each replication.

train.weights   List of lists of training weights for each Parafac or Parafac2 model and for each replication.

opt.tune   List of optimal tuning parameters for classification methods for each Parafac or Parafac2 model and for each replication.

mean.opt.tune	Mean across all replications of optimal tuning parameters for classification methods for each Parafac or Parafac2 model.
X	Three-way or four-way data array or list used in argument x.
nfac	Number of components used to fit each Parafac or Parafac2 model.
model	Character designating the Parafac model that was used, either model = "parafac" for the Parafac model or model = "parafac2" for the Parafac2 model.
method	Classification methods used.
const	Constraints used in fitting Parafac or Parafac2 models.
cmode	Integer value used to specify the mode whose component weights were predictors for classification.

Note

If argument cmode is not null, input array x is reshaped with function aperm such that the cmode dimension of x is ordered last. Estimated mode A and B (and mode C for a four-way array) weights that are outputted as Aweights and Bweights (and Cweights) reflect this permutation. For example, if x is a four-way array and cmode = 2, the original input modes 1, 2, 3, and 4 will correspond to output modes 1, 3, 4, 2. Here, output A = input 1; B = 3, and C = 4 (i.e., the second mode specified by cmode has been moved to the D mode/last mode). For model = "parafac2", classification mode is assumed to be the last mode (i.e., mode C for three-way array and mode D for four-way array).

In addition, note that the following combination of arguments will give an error: nfac = 1, family = "multinomial", method = "PLR". The issue arises from providing glmnet::cv.glmnet input x an input matrix that has a single column. The issue is resolved for family = "binomial" because a column of 0s is appended to the single column, but this solution does not appear to work for the multiclass case. As such, this combination of arguments is not currently allowed. Future updates are planned to resolve this issue.

Author(s)

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Examples

```
########## Parafac2 example with 4-way array and multiclass response ##########
## Not run:
# set seed
set.seed(5)

# define correlation matrix for columns of classification mode weight matrix
cormat <- matrix(c(1, .35, .35, .35, 1, .35, .35, .35, 1), nrow = 3, ncol = 3)

# simulate a four-way ragged array connected to a multiclass response
data <- simcpfa(arraydim = c(10, 11, 12, 100), model = "parafac2", nfac = 3,
                nclass = 3, nreps = 1e2, onreps = 10, corresp = rep(.75, 3),
                meanpred = rep(2, 3), modes = 4, corrpred = cormat)

# initialize
alpha <- seq(0, 1, length = 2)
gamma <- c(0, 1)
cost <- c(0.1, 5)
ntree <- c(200, 300)
nodesize <- c(1, 2)
size <- c(1, 2)
```

```
decay <- c(0, 1)
rda.alpha <- seq(0.1, 0.9, length = 2)
delta <- c(0.1, 2)
eta <- c(0.3, 0.7)
max.depth <- c(1, 2)
subsample <- c(0.75)
nrounds <- c(100)
method <- c("PLR", "SVM", "RF", "NN", "RDA", "GBM")
family <- "multinomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost, ntree = ntree,
                   nodesize = nodesize, size = size, decay = decay,
                   rda.alpha = rda.alpha, delta = delta, eta = eta,
                   max.depth = max.depth, subsample = subsample,
                   nrounds = nrounds)
model <- "parafac2"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal, fourth mode to be nonnegative
const <- c("orthog", "uncons", "uncons", "nonneg")

# fit Parafac2 model and use fourth mode weights to tune classification
# methods, to predict class labels, and to return classification
# performance measures pooled across multiple train-test splits
output <- cpfa(x = data$X, y = as.factor(data$y), model = model, nfac = 3,
               nrep = 5, ratio = 0.8, nfolds = nfolds, method = method,
               family = family, parameters = parameters,
               type.out = "descriptives", seeds = NULL, plot.out = TRUE,
               parallel = FALSE, const = const, nstart = nstart)

# print performance measure means across train-test splits
output$descriptive$mean

## End(Not run)
```

---

cpm	*Classification Performance Measures*

Description

Calculates multiple performance measures for binary or multiclass classification. Uses known class labels and evaluates against predicted labels.

Usage

```
cpm(x, y, level = NULL, fbeta = NULL, prior = NULL)
```

Arguments

x	Known class labels of class numeric, factor, or integer. If factor, converted to class integer in the order of factor levels with integers beginning at 0 (i.e., for binary classification, factor levels become 0 and 1; for multiclass, levels become 0, 1, 2, etc.).
y	Predicted class labels of class numeric, factor, or integer. If factor, converted to class integer in the order of factor levels with integers beginning at 0 (i.e., for binary classification, factor levels become 0 and 1; for multiclass, levels become 0, 1, 2, etc.).
level	Optional argument specifying possible class labels. For cases where x or y do not contain all possible classes. Can be of class numeric, integer, or character. Must contain two elements for binary classification, and contain three or more elements for multiclass classification. If integer, integers should be ordered (e.g., binary with c(0, 1); or three-class with c(0, 1, 2)). Note: if both x and y jointly contain only a single value (e.g., 1), must specify argument level in order to identify classification as binary or multiclass.
fbeta	Optional numeric argument specifying beta value for F-score. Defaults to fbeta = 1, providing an F1-score (i.e., the balanced harmonic mean between precision and recall). Can be any real number.
prior	Optional numeric argument specifying weights for classes. Currently only implemented with multiclass problems. Defaults to prior = c(rep(1/llev, llev)), where llev is the number of classes, providing equal importance across classes.

Details

Selecting one class as a negative class and one class as a positive class, binary classification generates four possible outcomes: (1) negative cases classified as positives, called false positives (FP); (2) negative cases classified as negatives, called true negatives (TN); (3) positive cases classified as negatives, called false negatives (FN); and (4) positive cases classified as positives, called true positives (TP).

Multiple evaluation measures are calculated using these four outcomes. Measures include: overall error (ERR), also called fraction incorrect; overall accuracy (ACC), also called fraction correct; true positive rate (TPR), also called recall, hit rate, or sensitivity; false negative rate (FNR), also called miss rate; false positive rate (FPR), also called fall-out; true negative rate (TNR), also called specificity or selectivity; positive predictive value (PPV), also called precision; false discovery rate (FDR); negative predictive value (NPV); false omission rate (FOR); and F-score (FS).

In multiclass classification, the four outcomes are possible for each individual class in macro-averaging, and performance measures are averaged over classes. Macro-averaging gives equal importance to all classes. For multiclass classification, calculated measures are currently only macro-averaged. See the listed reference in this help file for additional details on micro-averaging.

For binary classification, this function assumes a negative class and a positive class (i.e., it contains a reference group) and is ordered. Multiclass classification is currently assumed to be unordered.

Computational details:

ERR = (FP + FN) / (TP + TN + FP + FN).

ACC = (TP + TN) / (TP + TN + FP + FN), and ACC = 1 - ERR.

TPR = TP / (TP + FN).

FNR = FN / (FN + TP), and FNR = 1 - TPR.

FPR = FP / (FP + TN).

TNR = TN / (TN + FP), and TNR = 1 - FPR.

PPV = TP / (TP + FP).

FDR = FP / (FP + TP), and FDR = 1 - PPV.

NPV = TN / (TN + FN).

FOR = FN / (FN + TN), and FOR = 1 - NPV.

FS = (1 + beta^2) * ((PPV * TPR) / (((beta^2)*PPV) + TPR)).

All performance measures calculated are between 0 and 1, inclusive. For multiclass classification, macro-averaged values are provided for each performance measure. Note that 'beta' in FS represents the relative weight such that recall (TPR) is beta times more important than precision (PPV). See reference for more details.

Value

Returns list where first element is a full confusion matrix cm and where the second element is a data frame containing performance measures. For multiclass classification, macro-averaged values are provided (i.e., each measure is calculated for each class, then averaged over all classes; the average is weighted by argument prior if provided). The second list element contains the following performance measures:

cm	A confusion matrix with counts for each of the possible outcomes.
err	Overall error (ERR). Also called fraction incorrect.
acc	Overall accuracy (ACC). Also called fraction correct.
tpr	True positive rate (TPR). Also called recall, hit rate, or sensitivity.
fpr	False positive rate (FPR). Also called fall-out.
tnr	True negative rate (TNR). Also called specificity or selectivity.
fnr	False negative rate (FNR). Also called miss rate.
ppv	Positive predictive value (PPV). Also called precision.
npv	Negative predictive value (NPV).
fdr	False discovery rate (FDR).
fom	False omission rate (FOR).
fs	F-score. Mean between TPR (recall) and PPV (precision) varying by importance given to recall over precision (see Details section and argument fbeta).

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References

Sokolova, M. and Lapalme, G. (2009). A systematic analysis of performance measures for classification tasks. Information Processing and Management, 45(4), 427-437.

Examples

```
########## Parafac example with 3-way array and binary response ##########
## Not run:
# set seed and simulate a three-way array related to a binary response
set.seed(5)
cormat <- matrix(c(1, .35, .35, .35, 1, .35, .35, .35, 1), nrow = 3, ncol = 3)
data <- simcpfa(arraydim = c(10, 11, 100), model = "parafac", nfac = 3,
                nclass = 2, nreps = 1e2, onreps = 10, corresp = rep(.75, 3),
                meanpred = rep(2, 3), modes = 3, corrpred = cormat)

# initialize
alpha <- seq(0, 1, length = 2)
gamma <- c(0, 0.01)
cost <- c(1, 2)
method <- c("PLR", "SVM")
family <- "binomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost)
model <- "parafac"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal
const <- c("orthog", "uncons", "uncons")

# fit Parafac models and use third mode to tune classification methods
tune.object <- tunecpfa(x = data$X[, , 1:80], y = as.factor(data$y[1:80, ]),
                        model = model, nfac = 3, nfolds = nfolds,
                        method = method, family = family,
                        parameters = parameters, parallel = FALSE,
                        const = const, nstart = nstart)

# predict class labels
predict.labels <- predict(object = tune.object, newdata = data$X[, , 81:100],
                          type = "response")

# calculate performance measures for predicted class labels
y.pred <- predict.labels[, 1]
evalmeasure <- cpm(x = as.numeric(data$y[81:100, ]), y = y.pred)

# print performance measures
evalmeasure

## End(Not run)
```

---

cpm.all   *Wrapper for Calculating Classification Performance Measures*

Description

Applies function cpm to multiple sets of class labels. Each set of class labels is evaluated against the same set of predicted labels. Works with output from function predict.tunecpfa and calculates

classification performance measures for multiple classifiers or numbers of components.

Usage

```
cpm.all(x, y, ...)
```

Arguments

x	A data frame where each column contains a set of class labels of class numeric, factor, or integer. If a set is of class factor, that set is converted to class integer in the order of factor levels with integers beginning at 0 (i.e., for binary classification, factor levels become 0 and 1; for multiclass, levels become 0, 1, 2, etc.).
y	Class labels of class numeric, factor, or integer. If factor, converted to class integer in order of factor levels with integers beginning at 0 (i.e., for binary classification, factor levels become 0 and 1; for multiclass, 0, 1, 2, etc.).
...	Additional arguments passed to function cpm for calculating classification performance measures.

Details

Wrapper function that applies function cpm to multiple sets of class labels and one other set of labels. See help file for function cpm for additional details.

Value

Returns a list with the following two elements:

cm.list	A list of confusion matrices, denoted cm, where each confusion matrix is associated with one comparison.
cpms	A data frame containing classification performance measures where each row contains measures for one comparison.

Author(s)

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References

Sokolova, M. and Lapalme, G. (2009). A systematic analysis of performance measures for classification tasks. Information Processing and Management, 45(4), 427-437.

Examples

```
########## Parafac example with 3-way array and binary response ##########
## Not run:
# set seed and simulate a three-way array related to a binary response
set.seed(5)
cormat <- matrix(c(1, .35, .35, .35, 1, .35, .35, .35, 1), nrow = 3, ncol = 3)
data <- simcpfa(arraydim = c(10, 11, 100), model = "parafac", nfac = 3,
```

```
                        nclass = 2, nreps = 1e2, onreps = 10, corresp = rep(.75, 3),
                        meanpred = rep(2, 3), modes = 3, corrpred = cormat)

    # initialize
    alpha <- seq(0, 1, length = 2)
    gamma <- c(0, 0.01)
    cost <- c(1, 2)
    method <- c("PLR", "SVM")
    family <- "binomial"
    parameters <- list(alpha = alpha, gamma = gamma, cost = cost)
    model <- "parafac"
    nfolds <- 3
    nstart <- 3

    # constrain first mode weights to be orthogonal
    const <- c("orthog", "uncons", "uncons")

    # fit Parafac models and use third mode to tune classification methods
    tune.object <- tunecpfa(x = data$X[, , 1:80], y = as.factor(data$y[1:80, ]),
                            model = model, nfac = 3, nfolds = nfolds,
                            method = method, family = family,
                            parameters = parameters, parallel = FALSE,
                            const = const, nstart = nstart)

    # predict class labels
    predict.labels <- predict(object = tune.object, newdata = data$X[, , 81:100],
                              type = "response")

    # calculate performance measures for predicted class labels
    evalmeasure <- cpm.all(x = predict.labels, y = as.numeric(data$y[81:100, ]))

    # print performance measures
    evalmeasure

## End(Not run)
```

---

plotcpfa	*Plot Optimal Model from Classification with Parallel Factor Analysis*

Description

Plots optimal model based on results from a 'wrapcpfa' object generated by function cpfa.

Usage

```
plotcpfa(object, cmeasure = "acc", meanvalue = TRUE, supNum = FALSE,
         parallel = FALSE, cl = NULL, scale.remode = NULL, newscales = 1,
         scale.abmode = NULL, sign.remode = NULL, newsigns = 1,
         sign.abmode = NULL, ...)
```

Arguments

object	An object of class 'wrapcpfa' from function cpfa.
cmeasure	Classification performance measure used to select the optimal number of components. Options include c("err", "acc", "tpr", "fpr", "tnr", "fnr", "ppv", "npv", "fdr", "fom", "fs"). If cmeasure is in c("err", "fpr", "fnr", "fdr", "fom"), the number of components that minimized cmeasure is selected among all classification methods. Otherwise, the number that maximized cmeasure is selected.
meanvalue	Logical indicating whether to find the optimal number of components based on the mean performance across replications from the results generated by cpfa. If meanvalue = FALSE, the median is used.
supNum	Logical indicating whether to suppress text displaying component weight values within plot cells. If TRUE, values are not displayed.
parallel	Logical indicating whether parallel computing should be used. If TRUE, parallel computing is used.
cl	Cluster for parallel computing, which is used when parallel = TRUE. Note that if parallel = TRUE and cl = NULL, then the cluster is defined as makeCluster(detectCores()).
scale.remode	Character that indicates a mode to rescale. Must be one of c("A", "B", "C", "D"). Sent directly to argument mode in function rescale from package **multiway**. See help file for rescale for additional details.
newscales	The root mean-square for columns of the mode indicated by scale.remode. See help file for rescale for additional details.
scale.abmode	Character that indicates the mode that absorbs the inverse of rescalings applied to the mode indicated by scale.remode. Must be one of c("A", "B", "C", "D"). Sent directly to argument absorb in function rescale from package **multiway**. See help file for rescale for additional details.
sign.remode	Character that indicates a mode to resign. Must be one of c("A", "B", "C", "D"). Sent directly to argument mode in function resign from package **multiway**. See help file for resign for additional details.
newsigns	Scalar or vector indicating resignings for columns of the mode indicated by sign.remode. See help file for resign for additional details.
sign.abmode	Character that indicates the mode that absorbs the negation of the resignings applied to the mode indicated by sign.remode. Must be one of c("A", "B", "C", "D"). Sent directly to argument absorb in function resign from package **multiway**. See help file for resign for additional details.
...	Additional arguments to be passed to function parafac for fitting a Parafac model or function parafac2 for fitting a Parafac2 model. See help file for function parafac or for function parafac2 for additional details.

Details

Selects the number of components that optimized a performance measure across all classification methods used by cpfa. With this optimal number of components, fits the Parafac or Parafac2 model that was used by cpfa to create the input 'wrapcpfa' object. Uses same constraints used in cpfa. Plots component weights for this optimal model using heatmaps. Darker red indicates

component weights that are more negative while darker green indicates component weights that are more positive. For three-way Parafac, plots A and B weights. For four-way Parafac, plots A, B, and C weights. For three-way Parafac2, plots B weights. For four-way Parafac2, plots B and C weights.

Value

Returns one or more heatmap plots of component weights for the optimal Parafac or Parafac2 model. Returns list of estimated component weights used in the plots.

Author(s)

Matthew Snodgress <mattgress@protonmail.ch>

References

See help file for function `cpfa` for a list of references.

Examples

```
########## Parafac2 example with 4-way array and multiclass response ##########
## Not run:
# set seed and simulate a four-way ragged array related to a multiclass response
set.seed(5)
cormat <- matrix(c(1, .35, .35, .35, 1, .35, .35, .35, 1), nrow = 3, ncol = 3)
data <- simcpfa(arraydim = c(10, 11, 12, 100), model = "parafac2", nfac = 3,
                nclass = 3, nreps = 1e2, onreps = 10, corresp = rep(.75, 3),
                meanpred = rep(2, 3), modes = 4, corrpred = cormat)

# initialize
alpha <- seq(0, 1, length = 2)
gamma <- c(0, 1)
cost <- c(0.1, 5)
rda.alpha <- seq(0.1, 0.9, length = 2)
delta <- c(0.1, 2)
method <- c("PLR", "SVM", "RDA")
family <- "multinomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost,
                   rda.alpha = rda.alpha, delta = delta)
model <- "parafac2"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal, fourth mode to be nonnegative
const <- c("orthog", "uncons", "uncons", "nonneg")

# fit Parafac2 model and use fourth mode weights to tune classification
# methods, to predict class labels, and to return classification
# performance measures pooled across multiple train-test splits
output <- cpfa(x = data$X, y = as.factor(data$y), model = model, nfac = 3,
               nrep = 2, ratio = 0.8, nfolds = nfolds, method = method,
               family = family, parameters = parameters,
               type.out = "descriptives", seeds = NULL, plot.out = TRUE,
```

```
                    parallel = FALSE, const = const, nstart = nstart, ctol = 1e-2)

    # plot heatmap of component weights for optimal model
    plotcpfa(output, nstart = nstart, ctol = 1e-3)

    ## End(Not run)
```

---

predict.tunecpfa   *Predict Method for Tuning for Classification with Parallel Factor*
                            Analysis

Description

Obtains predicted class labels from a 'tunecpfa' model object generated by function tunecpfa.

Usage

```
## S3 method for class 'tunecpfa'
predict(object, newdata = NULL, method = NULL,
        type = c("response", "prob", "classify.weights"),
        threshold = NULL, ...)
```

Arguments

object	A fit object of class 'tunecpfa' produced by function tunecpfa.
newdata	An optional three-way or four-way data array used to predict Parafac or Parafac2 component weights using estimated Parafac or Parafac2 model component weights from the input object. For Parafac2, can be a list of length K where the k-th element is a matrix or three-way array associated with the k-th element. Array or list must contain only real numbers. Dimensions must match dimensions of original data for all modes except the classification mode. If omitted, the original data are used.
method	Character vector indicating classification methods to use. Possible methods include penalized logistic regression (PLR); support vector machine (SVM); random forest (RF); feed-forward neural network (NN); regularized discriminant analysis (RDA); and gradient boosting machine (GBM). If none selected, default is to use all methods.
type	Character vector indicating type of prediction to return. Possible values include: (1) "response", returning predicted class labels; (2) "prob", returning predicted class probabilities; or (3) "classify.weights", returning predicted component weights used for classification in the specified Parafac models. Defaults to "response".
threshold	For binary classification, value indicating prediction threshold over which observations are classified as the positive class. If not provided, calculates threshold using class proportions in original data. For multiclass classification, threshold is not currently implemented.
...	Additional predict arguments. Currently ignored.

Details

Predicts class labels for a binary or a multiclass outcome. Specifically, predicts component weights for one mode of a Parallel Factor Analysis-1 (Parafac) model or a Parallel Factor Analysis-2 (Parafac2) model using new data and previously estimated mode weights from original data. Passes predicted component weights to one or several classification methods as new data for predicting class labels.

Tuning parameters optimized by k-fold cross-validation are used for each classification method (see help for tunecpfa). If not supplied in argument threshold, prediction threshold for all classification methods is calculated using proportions of class labels for original data in the binary case (and the positive class proportion is set as the threshold). For multiclass case, class with highest probability is chosen.

Value

Returns one of the following, depending on the choice for argument type:

type = "response"

A data frame containing predicted class labels or probabilities (binary case) for each Parafac model and classification method selected (see argument type). Number of columns is equal to number of methods times number of Parafac models. Number of rows is equal to number of predicted observations.

type = "prob" A list containing predicted probabilities for each Parafac model and classification method selected (see argument type). Only returned if original response is multiclass (i.e., contained three or more class labels). The number of list elements is equal to the number of methods times the number of Parafac models.

type = "classify.weights"

List containing predicted component weights for each Parafac or Parafac2 model. Length is equal to number of Parafac models that were fit.

Author(s)

Matthew Snodgress <mattgress@protonmail.ch>

References

See help file for function tunecpfa for a list of references.

Examples

```
########## Parafac example with 3-way array and binary response ##########
## Not run:
# set seed and simulate a three-way array related to a binary response
set.seed(5)
cormat <- matrix(c(1, .35, .35, .35, 1, .35, .35, .35, 1), nrow = 3, ncol = 3)
data <- simcpfa(arraydim = c(10, 11, 100), model = "parafac", nfac = 3,
                nclass = 2, nreps = 1e2, onreps = 10, corresp = rep(.75, 3),
                meanpred = rep(2, 3), modes = 3, corrpred = cormat)

# initialize
alpha <- seq(0, 1, length = 2)
```

```
gamma <- c(0, 0.01)
cost <- c(1, 2)
method <- c("PLR", "SVM")
family <- "binomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost)
model <- "parafac"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal
const <- c("orthog", "uncons", "uncons")

# fit Parafac models and use third mode to tune classification methods
tune.object <- tunecpfa(x = data$X[, , 1:80], y = as.factor(data$y[1:80, ]),
                        model = model, nfac = 3, nfolds = nfolds,
                        method = method, family = family,
                        parameters = parameters, parallel = FALSE,
                        const = const, nstart = nstart)

# predict class labels
predict.labels <- predict(object = tune.object, newdata = data$X[, , 81:100],
                          type = "response")

# print predicted labels
predict.labels

## End(Not run)
```

| print.tunecpfa | *Print Method for Tuning for Classification with Parallel Factor Analysis* |

Description

Prints summary of a 'tunecpfa' model object generated by function tunecpfa.

Usage

```
## S3 method for class 'tunecpfa'
print(x, ...)
```

Arguments

x   A fit object of class 'tunecpfa' from function tunecpfa.

...   Additional print arguments.

Details

Prints names of the models and methods used to create the input 'tunecpfa' model object. Prints misclassification error rates and estimation times in seconds.

Value

Returns a summary of the 'tunecpfa' model object.

Author(s)

Matthew Snodgress <mattgress@protonmail.ch>

References

See help file for function `tunecpfa` for a list of references.

Examples

```
########## Parafac example with 3-way array and binary response ##########
## Not run:
# set seed and simulate a three-way array connected to a binary response
set.seed(5)
cormat <- matrix(c(1, .35, .35, .35, 1, .35, .35, .35, 1), nrow = 3, ncol = 3)
data <- simcpfa(arraydim = c(10, 11, 80), model = "parafac", nfac = 3,
                nclass = 2, nreps = 1e2, onreps = 10, corresp = rep(.75, 3),
                meanpred = rep(2, 3), modes = 3, corrpred = cormat)

# initialize
alpha <- seq(0, 1, length = 2)
gamma <- c(0, 0.01)
cost <- c(1, 2)
method <- c("PLR", "SVM")
family <- "binomial"
parameters <- list(alpha = alpha, gamma = gamma, cost = cost)
model <- "parafac"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal
const <- c("orthog", "uncons", "uncons")

# fit Parafac models and use third mode to tune classification methods
tune.object <- tunecpfa(x = data$X, y = as.factor(data$y), model = model,
                        nfac = 3, nfolds = nfolds, method = method,
                        family = family, parameters = parameters,
                        parallel = FALSE, const = const, nstart = nstart)

# print summary of output
print(tune.object)

## End(Not run)
```

---

simcpfa   *Simulate Data for Classification with Parallel Factor Analysis*

Description

Simulates a three-way or four-way data array and a set of class labels that are related to the simulated array through one mode of the array. Data array is simulated using either a Parafac or Parafac2 model with no constraints. Weights for mode weight matrices can be drawn from 12 common probability distributions. Alternatively, custom weights can be provided for any mode.

Usage

```
simcpfa(arraydim = NULL, model = "parafac", nfac = 2, nclass = 2, nreps = 100,
        onreps = 10, corresp = c(0.3, -0.3), meanpred = c(0, 0), modes = 3,
        corrpred = matrix(c(1, 0.2, 0.2, 1), nrow = 2), pf2num = NULL,
        Amat = NULL, Bmat = NULL, Cmat = NULL, Dmat = NULL, Gmat = NULL,
        Emat = NULL, technical = list())
```

Arguments

arraydim	Numeric vector containing the number of dimensions for each mode of the simulated data array. Must contain integers greater than or equal to 2.
model	Character specifying the model to use for simulating the data array. Must be either 'parafac' or 'parafac2'.
nfac	Number of components in the Parafac or Parafac2 model. Must be an integer greater than or equal to 1.
nclass	Number of classes in simulated class labels. Must be an integer greater than or equal to 2.
nreps	Number of replications for simulating class labels for a given set of classification mode component weights.
onreps	Number of replications for simulating a set of classification mode component weights.
corresp	Numeric vector of target correlations between simulated class labels and columns of the classification mode component weight matrix. Must have length equal to 'nfac'.
meanpred	Numeric vector of means used to generate the classification mode component weights. Must be real numbers. Operates as the mean vector parameterizing a multivariate normal distribution from which classification mode component weights are generated. Length must be equal to input `nfac`.
modes	Single integer of either 3 or 4, indicating whether to simulate a three-way or four-way data array, respectively.
corrpred	A positive definite correlation matrix containing the target correlations for the classification mode component weights. Must have number of rows and columns equal to input 'nfac'. Operates as the covariance matrix parameterizing a multivariate normal distribution from which classification mode component weights are generated.

pf2num	When `model = 'parafac2'`, number of rows for each simulated matrix in the list of matrices `Amat`. Replaces the first element of input `arraydim` because, for the Parafac2 model, the number of rows in each simulated matrix can vary. If not specified when `model = 'parafac2'`, defaults to `rep(c((nfac + 1), (nfac + 2), (nfac + 3)), length.out = arraydim[modes])`.
Amat	When `model = 'parafac'`, a matrix of A mode weights with number of rows equal to the first element of input 'arraydim' and with number of columns equal to input 'nfac'. When `model = 'parafac2'`, a list with length equal to the last element of input 'arraydim', where each list element contains a matrix with number of rows of at least 2 and with number of columns equal to input 'nfac'. When provided, replaces a simulated `Amat`.
Bmat	A matrix of B mode weights with number of rows equal to the second element of input 'arraydim' and with number of columns equal to the input 'nfac'. When provided, replaces a simulated `Bmat`.
Cmat	A matrix of C mode weights with number of rows equal to the third element of input 'arraydim' and with number of columns equal to the input 'nfac'. When provided, replaces a simulated `Cmat` when `modes = 4`. When `modes = 3`, replaces the simulated classification mode weight matrix. If provided when `modes = 3`, `onreps` is reduced to one.
Dmat	A matrix of D mode weights with number of rows equal to the fourth element of input 'arraydim' and with number of columns equal to the input 'nfac'. When `modes = 4`, replaces the simulated classification mode weight matrix. When `modes = 3`, this argument is ignored. If provided when `modes = 4`, `onreps` is reduced to one.
Gmat	When `model = 'parafac2'`, a matrix of G mode weights with number of rows equal to input 'nfac' and with number of columns equal to input 'nfac'. When provided, replaces a simulated `Gmat`.
Emat	When `model = 'parafac'`, an array containing noise to be added to the corresponding elements in the simulated data array. Error array dimensions must be equal to the values contained in `arraydim`. When `model = 'parafac2'`, a list containing either matrices (i.e., when `modes = 3`) or three-way arrays (i.e., when `modes = 4`) whose elements contain noise to be added to corresponding elements in the simulated data array. When provided, replaces a simulated `Emat`.
technical	List containing arguments related to distributions from which to simulate data. When specified, must contain one or more of the following:

> **distA** List containing arguments specifying the distribution from which deviates are drawn for A mode weights contained in `Amat`. Defaults to standard normal distribution when not specified. See Details section for additional information on acceptable arguments.
>
> **distB** List containing arguments specifying the distribution from which deviates are drawn for B mode weights contained in `Bmat`. Defaults to standard normal distribution when not specified. See Details section for additional information on acceptable arguments.
>
> **distC** For when `modes = '4'`, list containing arguments specifying the distribution from which deviates are drawn for C mode weights contained in `Cmat`. Defaults to standard normal distribution when not specified. See Details section for additional information on acceptable arguments.

distG For when `model = 'parafac2'`, list containing arguments specifying the distribution from which deviates are drawn for G weights contained in `Gmat`. Defaults to standard normal distribution when not specified. See Details section for additional information on acceptable arguments.

distE List containing arguments specifying the distribution from which deviates are drawn for error contained in `Emat`. Defaults to standard normal distribution when not specified. See Details section for additional information on acceptable arguments.

Details

Data array simulation consists of two steps. First, a Monte Carlo simulation is conducted to simulate class labels using a binomial logistic (i.e., in the binary case) or multinomial logistic (i.e., in the multiclass case) regression model. Specifically, columns of the classification mode weights matrix (e.g., `Cmat` when `modes = 3`) are generated from a multivariate normal distribution with mean vector `meanpred` and with covariance matrix `corrpred`. Values are then drawn randomly from a uniform or a normal distribution and serve as beta coefficients. A linear combination of these beta coefficients and the generated classification weights produces a linear systematic part, which is passed through the logistic function (i.e., the sigmoid) in the binary case or through the softmax function in the multiclass case. Resulting probabilities are used to assign class labels. The simulation repeats classification weights generation `onreps` times and repeats class label generation, within each `onreps` iteration, a total of `nreps` times. The generated class labels that correlate best with the generated classification weights (i.e., with correlations closest to `corresp`) are retained as the final class labels with corresponding final classification weights. An adaptive sampling technique is used during the simulation such that optimal beta coefficients from previous iterations are used to parameterize a normal distribution, from which new coefficients are drawn in subsequent iterations. Note that, if any simulation replicate produces a set of class labels where all labels are the same (i.e., have no variance), that replicate is discarded. Note also that `onreps` is ignored when the classification mode weight matrix (i.e., `Cmat` when `modes = 3` or `Dmat` when `modes = 4`) is provided; in this case, class labels are simulated with respect to the provided classification mode weight matrix.

Second, depending on the chosen model (i.e., Parafac or Parafac2) specified via `model`, and depending on the number of modes specified via `modes`, component matrices are randomly generated for each mode of the data array. A data array is then constructed using a Parafac or Parafac2 structure from these weight matrices, including the generated classification mode weight matrix (i.e., `Cmat` or `Dmat`) from the first step. Alternatively, weight matrices can be provided to override random generation for any weight matrix with the exception of the classification mode. When provided, weight matrices are used to form the final data array. Finally, random noise is added to each value in the array. The resulting output is a synthetic multiway data array paired, through one mode of the array, with a simulated binary or multiclass response.

The `technical` argument controls the probability distributions used to simulate weights for different modes. Currently, `technical` is highly structured. In particular, `technical` must be provided as a named list whose elements must be one of 'distA', 'distB', 'distC', 'distG', or 'distE', with the last letter of each name designating a mode or, in the case of 'distE', designating error. Each element provided must itself be a list where the first inner list element is named 'dname', specifying the distribution to be used to generate weights for a given mode or for error. There are 12 'dname' options: 'normal', 'uniform', 'gamma', 'beta', 'binomial', 'poisson', 'exponential', 'geometric', 'negbinomial', 'hypergeo', 'lognormal', and 'cauchy'. Additional arguments can be added to each inner list to parameterize the probability distribution being used. These arguments can be one of the

following, for each distribution allowed:

For dname = 'normal', allowed arguments are mean or sd (i.e., function rnorm is called).

For dname = 'uniform', allowed arguments are min or max (i.e., function runif is called).

For dname = 'gamma', allowed arguments are shape or scale (i.e., function rgamma is called).

For dname = 'beta', allowed arguments are shape1 or shape2 (i.e., function rbeta is called).

For dname = 'binomial', allowed arguments are size or prob (i.e., function rbinom is called).

For dname = 'poisson', allowed argument is lambda (i.e., function rpois is called).

For dname = 'exponential', allowed argument is rate (i.e., function rexp is called).

For dname = 'geometric', allowed argument is prob (i.e., function rgeom is called).

For dname = 'negbinomial', allowed arguments are size or prob (i.e., function rnbinom is called).

For dname = 'hypergeo', allowed arguments are m, n, or k (i.e., function rhyper is called).

For dname = 'lognormal', allowed arguments are meanlog or sdlog (i.e., function rlnorm is called).

For dname = 'cauchy', allowed arguments are location or scale (i.e., function rcauchy is called).

Note that if a weight matrix and technical information are both provided for a given mode (or for error), the weight matrix is used while technical information is ignored. See Examples below for an example of how to set up technical.

Value

X	Simulated data array with dimensions specified by arraydim and, when model = 'parafac2', also by pf2num. When model = 'parafac', X is an object of class 'array'. When model = 'parafac2', X is an object of class 'list'.
y	Simulated class labels provided as an object of class 'matrix', with number of rows equal to the last element of arraydim and with number of columns equal to 1.
model	Character value indicating whether Parafac or Parafac2 model was used to simulate the data array.
Amat	Simulated A mode weights. When model = 'parafac', output is a matrix with number of rows equal to the first element of arraydim and with number of columns equal to the number of components nfac. When model = 'parafac2', output is a list of matrices with number of rows for each matrix equal to those specified by pf2num and with number of columns equal to nfac. If Amat was supplied, returns original Amat instead of a simulated Amat.
Bmat	Simulated B mode weights provided as a matrix with number of rows equal to the second element of arraydim and with number of columns equal to the number of components nfac. If Bmat was supplied, returns original Bmat instead of a simulated Bmat.
Cmat	Simulated C mode weights provided as a matrix with number of rows equal to the third element of arraydim and with number of columns equal to the number of components nfac. If Cmat was supplied when modes = 4, returns original Cmat instead of a simulated Cmat.

Dmat	Simulated D mode weights provided when modes = 4. Output is a matrix with number of rows equal to the fourth element of arraydim and with number of columns equal to the number of components nfac.
Gmat	Simulated G weights provided when model = 'parafac2'. Provided as a matrix with number of rows and columns equal to nfac. If Gmat was supplied, returns original Gmat instead of a simulated Gmat.
Emat	Error array or list containing noise added to corresponding elements of simulated data array. Output has dimensions specified by arraydim and, when model = 'parafac2', also by pf2num. When model = 'parafac', Emat is an object of class 'array'. When model = 'parafac2', Emat is an object of class 'list'.

Note

This simulation implementation contains at least two limitations. First, there is currently no argument to control the proportions of generated class labels. Second, the covariance matrix parameterizing the multivariate normal distribution generating classification mode weights is restricted to a correlation matrix. Future updates are planned to address these limitations.

In addition, the simulation could be expanded in at least two ways. First, the Monte Carlo simulation, as a brute-force strategy, is simple but not optimal and could be replaced with a more efficient approach. Note that the correlations between simulated class labels and classification mode weights, while ideally close to corresp, represent a best-case scenario—given values for onreps, nreps, and corrpred. Second, class labels are currently connected to the data array through only one mode but could be simulated such that they are connected through two or more modes. Future updates are planned to implement these enhancements.

Author(s)

Matthew Snodgress <mattgress@protonmail.ch>

References

See help file for function cpfa for a list of references.

Examples

```
########## Parafac2 example with 4-way array and multiclass response ##########
## Not run:
# set seed for reproducibility
set.seed(5)

# define list of arguments specifying distributions for A and G weights
techlist <- list(distA = list(dname = "poisson",
                             lambda = 3),              # for A weights
                distG = list(dname = "gamma", shape = 2,
                             scale = 4))               # for G weights

# define target correlation matrix for columns of D mode weights matrix
cormat <- matrix(c(1, .35, .35, .35, 1, .35, .35, .35, 1), nrow = 3, ncol = 3)

# simulate a four-way ragged array connected to a response
```

```
data <- simcpfa(arraydim = c(10, 11, 12, 100), model = "parafac2", nfac = 3,
                nclass = 3, nreps = 1e2, onreps = 10, corresp = rep(.75, 3),
                meanpred = rep(2, 3), modes = 4, corrpred = cormat,
                technical = techlist)

# examine correlations among columns of classification mode matrix Dmat
cor(data$Dmat)

# examine correlations between columns of classification mode matrix Dmat and
# simulated class labels
cor(data$Dmat, data$y)

## End(Not run)
```

---

tunecpfa   *Tuning for Classification with Parallel Factor Analysis*

Description

Fits Richard A. Harshman's Parallel Factor Analysis-1 (Parafac) model or Parallel Factor Analysis-2 (Parafac2) model to a three-way or four-way data array. Allows for multiple constraint options on tensor modes. Uses component weights from a single mode of the model as predictors to tune parameters for one or more classification methods via a k-fold cross-validation procedure. Supports binary and multiclass classification.

Usage

```
tunecpfa(x, y, model = c("parafac", "parafac2"), nfac = 1, nfolds = 10,
         method = c("PLR", "SVM", "RF", "NN", "RDA", "GBM"),
         family = c("binomial", "multinomial"), parameters = list(),
         foldid = NULL, prior = NULL, cmode = NULL, parallel = FALSE,
         cl = NULL, verbose = TRUE, ...)
```

Arguments

x	For Parafac or Parafac2, a three-way or four-way data array. For Parafac2, can be a list where each element is a matrix or three-way array. Array or list must contain real numbers. See note below.
y	A vector containing at least two unique class labels. Should be a factor that contains two or more levels. For binary case, ensure the order of factor levels (left to right) is such that negative class is first and positive class is second.
model	Character designating the Parafac model to use, either model = "parafac" to fit the Parafac model or model = "parafac2" to fit the Parafac2 model.
nfac	Number of components for each Parafac or Parafac2 model to fit. Default is nfac = 1.
nfolds	Numeric value specifying the number of folds for k-fold cross-validation. Must be 2 or greater. Default is nfolds = 10.

method   Character vector indicating classification methods to use. Possible methods in-
                clude penalized logistic regression (PLR); support vector machine (SVM); ran-
                dom forest (RF); feed-forward neural network (NN); regularized discriminant
                analysis (RDA); and gradient boosting machine (GBM). If none selected, de-
                fault is to use all methods.

family   Character value specifying binary classification (family = "binomial") or mul-
                ticlass classification (family = "multinomial"). If not provided, number of
                levels of input y is used, where two levels is binary, and where three or more
                levels is multiclass.

parameters   List containing arguments related to classification methods. When specified,
                must contain one or more of the following:

                alpha Values for penalized logistic regression alpha parameter; default is alpha
                = seq(0, 1, length = 6). Must be numeric and contain only real numbers
                between 0 and 1, inclusive.

                lambda Optional user-supplied lambda sequence for cv.glmnet for penalized
                logistic regression. Default is NULL.

                cost Values for support vector machine cost parameter; default is cost = c(1,
                2, 4, 8, 16, 32, 64). Must be numeric and contain only real numbers
                greater than or equal to 0.

                gamma Values for support vector machine gamma parameter; default is gamma
                = c(0, 0.01, 0.1, 1, 10, 100, 1000). Must be numeric and greater than
                or equal to 0.

                ntree Values for random forest number of trees parameter; default is ntree =
                c(100, 200, 400, 600, 800, 1600, 3200). Must be numeric and contain
                only integers greater than or equal to 1.

                nodesize Values for random forest node size parameter; default is nodesize
                = c(1, 2, 4, 8, 16, 32, 64). Must be numeric and contain only integers
                greater than or equal to 1.

                size Values for neural network size parameter; default is size = c(1, 2, 4, 8,
                16, 32, 64). Must be numeric and contain only integers greater than or
                equal to 0.

                decay Values for neural network decay parameter; default is decay = c(0.001,
                0.01, 0.1, 1, 2, 4, 8, 16). Must be numeric and contain only real num-
                bers.

                rda.alpha Values for regularized discriminant analysis alpha parameter; default
                is rda.alpha = seq(0, 0.999, length = 6). Must be numeric and contain
                only real numbers between 0 (inclusive) and 1 (exclusive).

                delta Values for regularized discriminant analysis delta parameter; default is
                delta = c(0, 0.1, 1, 2, 3, 4). Must be numeric and contain only real
                numbers greater than or equal to 0.

                eta Values for gradient boosting machine eta parameter; default is eta = c(0.1,
                0.3, 0.5, 0.7, 0.9). Must be numeric and contain only real numbers
                greater than 0 and less than 1.

                max.depth Values for gradient boosting machine max.depth parameter; default
                is max.depth = c(1, 2, 3, 4). Must be numeric and contain only integers
                greater than or equal to 1.

       subsample Values for gradient boosting machine subsample parameter; default is subsample = c(0.6, 0.7, 0.8, 0.9). Must be numeric and contain only real numbers greater than 0 and less than or equal to 1.

       nrounds Values for gradient boosting machine nrounds parameter; default is nrounds = c(100, 200, 300, 500). Must be numeric and contain only integers greater than or equal to 1.

foldid   Vector containing fold IDs for k-fold cross-validation. Can be of class integer, numeric, or data frame. Should contain integers from 1 through the number of folds. If not provided, fold IDs are generated randomly for observations using 1 through the number of folds nfolds.

prior   Prior probabilities of class membership. If unspecified, the class proportions for input y are used. If specified, the probabilities should be in the order of the factor levels of input y.

cmode   Integer value of 1, 2, or 3 (or 4 if x is a four-way array) specifying the mode whose component weights will be predictors for classification. Defaults to the last mode of the input array (i.e., defaults to 3 for three-way array, and to 4 for four-way array). If model = "parafac2", last mode will be used.

parallel   Logical indicating whether to use parallel computing. If TRUE, the package **parallel** is used for parallel computing. For all classification methods except penalized logistic regression, the **doParallel** package is used as a wrapper. Defaults to FALSE, which implements sequential computing.

cl   Cluster for parallel computing, which is used when parallel = TRUE. Note that if parallel = TRUE and cl = NULL, then the cluster is defined as makeCluster(detectCores()).

verbose   If TRUE, progress is printed.

...   Additional arguments to be passed to function parafac for fitting a Parafac model or function parafac2 for fitting a Parafac2 model. Example: can impose different constraints on different modes of the input array using the argument const. See help file for function parafac or for function parafac2 for additional details.

Details

After fitting a Parafac or Parafac2 model using package **multiway** (see parafac or parafac2 in **multiway** for details), the estimated classification mode weight matrix is passed to one or more classification methods–including penalized logistic regression (PLR); support vector machine (SVM); random forest (RF); feed-forward neural network (NN); regularized discriminant analysis (RDA); and gradient boosting machine (GBM).

Package **glmnet** fits models for PLR. PLR tunes penalty parameter lambda while the elastic net parameter alpha is set by the user (see the help file for function cv.glmnet in package **glmnet**). For SVM, package **e1071** is used with a radial basis kernel. Penalty parameter cost and radial basis parameter gamma are used (see svm in package **e1071**). For RF, package **randomForest** is used and implements Breiman's random forest algorithm. The number of predictors sampled at each node split is set at the default of sqrt(R), where R is the number of Parafac or Parafac2 components. Two tuning parameters allowed are ntree, the number of trees to be grown, and nodesize, the minimum size of terminal nodes (see randomForest in package **randomForest**). For NN, package **nnet** fits a single-hidden-layer, feed-forward neural network model. Penalty parameters size (i.e.,

number of hidden layer units) and decay (i.e., weight decay) are used (see **nnet**). For RDA, package **rda** fits a shrunken centroids regularized discriminant analysis model. Tuning parameters include rda.alpha, the shrinkage penalty for the within-class covariance matrix, and delta, the shrinkage penalty of class centroids towards the overall dataset centroid. For GBM, package **xgboost** fits a gradient boosting machine model. Four tuning parameters are allowed: (1) eta, the learning rate; (2) max.depth, the maximum tree depth; (3) subsample, the fraction of samples per tree; and (4) nrounds, the number of boosting trees to build.

For all six methods, k-fold cross-validation is implemented to tune classification parameters where the number of folds is set by argument nfolds.

Value

Returns an object of class tunecpfa with the following elements:

opt.model	List containing optimal model for tuned classification methods for each Parafac or Parafac2 model that was fit.
opt.param	Data frame containing optimal parameters for tuned classification methods.
kcv.error	Data frame containing KCV misclassification error for optimal parameters for tuned classification methods.
est.time	Data frame containing times for fitting Parafac or Parafac2 model and for tuning classification methods.
method	Numeric indicating classification methods used. Value of '1' indicates 'PLR'; value of '2' indicates 'SVM'; value of '3' indicates 'RF'; value of '4' indicates 'NN'; value of '5' indicates 'RDA'; and value of '6' indicates 'GBM'.
x	Three-way or four-way array used. If a list was used with model = "parafac2", returns list of matrices or three-way arrays used.
y	Factor containing class labels used. Note that output y is recoded such that the input labels of y are converted to numeric integers from 0 through the number of levels, which are then applied as labels for output y.
Aweights	List containing estimated A weights for each Parafac or Parafac2 model that was fit.
Bweights	List containing estimated B weights for each Parafac or Parafac2 model that was fit.
Cweights	List containing estimated C weights for each Parafac or Parafac2 model that was fit. Null if input argument x was a three-way array.
Phi	If model = "parafac2", a list containing estimated Phi from the Parafac2 model. Phi is the common cross product matrix shared by all levels of the last mode (see help file for function parafac2 in package **multiway** for additional details). NULL if model = "parafac".
const	Constraints used in fitting Parafac or Parafac2 models. If argument const was not provided, no constraints will be used.
cmode	Integer value of 1, 2, or 3 (or 4 if x is a four-way array) specifying mode whose component weights were predictors for classification.
family	Character value specifying whether classification was binary (family = "binomial") or multiclass (family = "multinomial").

xdim	Numeric value specifying number of levels for each mode of input x. If model = "parafac2", number of levels for first mode is designated as NA because the number of levels can differ across levels of the last mode.
lxdim	Numeric value specifying number of modes of input x.
train.weights	List containing classification component weights for each fit Parafac or Parafac2 model, for possibly different numbers of components. The weights used to train classifiers.

Note

For fitting the Parafac model, if argument cmode is not NULL, input array x is reshaped with function aperm such that the cmode dimension of x is ordered last. Estimated mode A and B (and mode C for a four-way array) weights that are outputted as Aweights and Bweights (and Cweights) reflect this permutation. For example, if x is a four-way array and cmode = 2, the original input modes 1, 2, 3, and 4 will correspond to output modes 1, 3, 4, 2. Here, output A = input 1; B = 3, and C = 4 (i.e., the second mode specified by cmode has been moved to the D mode/last mode). For model = "parafac2", classification mode is assumed to be the last mode (i.e., mode C for three-way array and mode D for four-way array).

In addition, note that the following combination of arguments will give an error: nfac = 1, family = "multinomial", method = "PLR". The issue arises from providing glmnet::cv.glmnet input x with a matrix that has a single column. The issue is resolved for family = "binomial" because a column of 0s is appended to the single column, but this solution does not appear to work for the multiclass case. As such, this combination of arguments is not currently allowed. This issue will be resolved in a future update.

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Examples

```
########## Parafac example with 3-way array and binary response ##########
## Not run:
# set seed and simulate a three-way array connected to a binary response
set.seed(5)
cormat <- matrix(c(1, .35, .35, .35, 1, .35, .35, .35, 1), nrow = 3, ncol = 3)
data <- simcpfa(arraydim = c(10, 11, 80), model = "parafac", nfac = 3,
                nclass = 2, nreps = 1e2, onreps = 10, corresp = rep(.75, 3),
                meanpred = rep(2, 3), modes = 3, corrpred = cormat)

# initialize
alpha <- seq(0, 1, length = 2)
gamma <- c(0, 0.01)
cost <- c(1, 2)
ntree <- c(100, 200)
nodesize <- c(1, 2)
size <- c(1, 2)
decay <- c(0, 1)
rda.alpha <- c(0.1, 0.6)
delta <- c(0.1, 2)
eta <- c(0.3, 0.7)
max.depth <- c(1, 2)
subsample <- c(0.75)
nrounds <- c(100)
method <- c("PLR", "SVM", "RF", "NN", "RDA", "GBM")
family <- "binomial"
```

```
parameters <- list(alpha = alpha, gamma = gamma, cost = cost, ntree = ntree,
                    nodesize = nodesize, size = size, decay = decay,
                    rda.alpha = rda.alpha, delta = delta, eta = eta,
                    max.depth = max.depth, subsample = subsample,
                    nrounds = nrounds)
model <- "parafac"
nfolds <- 3
nstart <- 3

# constrain first mode weights to be orthogonal
const <- c("orthog", "uncons", "uncons")

# fit Parafac models and use third mode to tune classification methods
tune.object <- tunecpfa(x = data$X, y = as.factor(data$y), model = model,
                        nfac = 3, nfolds = nfolds, method = method,
                        family = family, parameters = parameters,
                        parallel = FALSE, const = const, nstart = nstart)

# print tuning object
tune.object

## End(Not run)
```

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